1 Optimizing mHealth Interventions with a Bandit (Preprint)

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23 Abstract

24 Mobile health (mHealth) interventions can enable new ways to improve health outcomes by 25 intervening in the moment of need or in the right life circumstance. With recent advances in 26 mobile computing and sensing techniques, mHealth interventions are now technologically 27 feasible; current off-the-shelf mobile phones can acquire and process data in real time to deliver 28 relevant interventions in the moment. Learning which intervention to provide in the moment, 29 however, is an optimization problem. This book chapter describes one algorithmic approach, a 30 "bandit algorithm," to optimize mHealth interventions. Bandit algorithms are well-studied and 31 are commonly used in online recommendations (e.g., Google's ad placement, or news 32 recommendations). Below, we walk through simulated and real-world examples to demonstrate 33 how bandit algorithms can be used to personalize and contextualize mHealth interventions. We 34 conclude by discussing challenges in developing bandit-based mobile health interventions.

35

36 1. Introduction

37 Before mHealth, the standard of care was periodic visits to a clinician's office, interspersed with 38 little to no patient support in between visits. At the clinician's office, data is collected to 39 describe the patient's state at that visit time and self-report data about the patient's state prior to 40 the current visit time is collected through an error-prone mechanism of recalling past events. 41 The mHealth model has enabled significant progress in-situ data collection between clinic visits; 42 phone sensors can now capture personal data at a millisecond level, and improvement in user 43 interfaces has reduced the burden of self-report information [18]. mHealth interventions using 44 persuasive design features are promising approaches for improving patients health [19,20].

However providing effective interventions personalized to the patient between patient visitsremains challenging.

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48 Two key components of intervening at the right time are personalization and contextualization. 49 Personalization is the process of matching an individual's preferences and lifestyle. e.g., a 50 physical activity intervention can say, "You walked 10 times in the last week near your office. 51 Don't forget to take small walks near your office today." Such personalization can lower barriers 52 to acting on the suggestion [2]. Contextualization takes personalization one step further by 53 delivering interventions at moments of need or at an opportune moment when the intervention is 54 easy to follow [1]. e.g., when a participant reaches the office, a push notification with the earlier 55 walking suggestion can be sent, or, just after a high risk teen reports high stress, a SMS can be 56 sent with ideas to reduce stress.

57

58 Contextualization and personalization, are complex problems because different people may 59 prefer different interventions and these preferences can vary by context. Fortunately, similar 60 problems have been solved before. When Google places ads or Netflix suggests movies, they 61 adapt their recommendation based on user preferences and characteristics, utilizing bandit 62 algorithms. Here we describe how bandit algorithms can be repurposed to personalize and 63 contextualize mHealth interventions. We will start with a simple example, where we personalize 64 a daily list of physical activity suggestions to an individual. We will then extend this simple 65 example to account for contextual factors (e.g., weather). We conclude with a real-world 66 example and discuss future challenges in developing personalized/contextualized interventions 67 with bandit algorithms.

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69

70 2. Background

71 Bandit algorithms: "Bandit algorithms" are so called because they were first devised for the 72 situation of a gambler playing one-armed bandits (slot machines with a long arm on the side 73 instead of a push button). Each time the gambler picks a slot machine, he/she receives a reward. 74 The bandit problem is to learn how to best sequentially select slot machines so as to maximize 75 total rewards. The fundamental issue of bandit problems is the *exploitation-exploration* tradeoff; 76 here exploitation means re-using highly rewarding slot machines from the past and exploration 77 means trying new or less-used slot machines to gather more information. While exploration may 78 yield less short-term payoff, an exploitation-only approach may miss a highly rewarding slot machine. Researchers have proposed solutions to the bandit's exploit-explore tradeoff across 79 80 many areas. In particular, once the relevance of bandit algorithms to internet advertising was 81 understood, there was a flurry of work [4]. Nowadays, bandit algorithms are theoretically well 82 understood, and their benefits have been empirically demonstrated [4,5].

83

An important class of bandit problems is the contextual bandit problem that considers additional contextual information in selecting the slot machine [6]. Contextual bandit problems provide a natural model for developing mobile health interventions. In this model the context is the information about the individual's current circumstances, the slot machines correspond to the different intervention options, and the rewards are near-time, proximal, outcomes [3]. In this setup, optimizing mHealth intervention delivery is the act of learning the intervention option that 90 will result in the best proximal outcome in a given circumstance. This is same as solving the91 contextual bandit problem.

92

93 **3.** Optimizing intervention with a Bandit algorithm

- 94 We will use two examples to explain how bandits can be used to optimize an mHealth
- 95 intervention for an individual. In section 4, we will discuss another real-world mobile application

96 that builds on the ideas introduced in the first two simple examples.

97

98 In our first example, the bandit algorithm will be used to select an optimal set of five physical

99 activity suggestions, for an individual, from a set of ten suggestions. A set of five suggestions is

100 optimal if the set leads to the highest level of daily activity for that individual. The second

101 example extends the first by finding a set of five suggestions for each of several contexts.

102 Contextualizing suggestions can be helpful because the same suggestion may be more actionable

103 in certain contexts (e.g., good weather or day of the week).

- 1. Walk 30 minutes
- 2. Add intervals: walk 5 minutes, walk very fast for 5 minutes, repeat 3 times
- 3. Take the stairs instead of the elevator whenever possible
- 4. Go for a walk with a friend or your dog
- 5. Swim a lap, rest 1 minute, repeat 10 times
- 6. Attend a fitness class at your gym

7.	Try some of the strength training and bodyweight exercises illustrated by the fitness
	app on your phone

8. Do yoga

- 9. Park at the far end of the parking lot to walk farther
- 10. Do yardwork for at least 10 minutes

Table 1: List of 10 suggestions

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107 **3.1 Personalizing suggestions for an individual**

108 Consider a scenario in which Jane's health plan gives her a physical activity tracker and a 109 smartphone app. Jane's health plan has found that the ten activity suggestions from Table 1 often 110 work for many less-active people to increase their activity. Note that the order of suggestions in 111 Table 1 does not imply any specific ranking. It is unlikely, however, that every individual will be 112 able to follow or prefer to follow all the 10 suggestions equally and there will be inter-personal 113 variability in which suggestions are followed and to what degree. Thus, we set the goal of 114 learning the five suggestions with the highest chance of maximizing Jane's activity. We use the 115 bandit algorithm, which is running as part of Jane's smartphone app, to achieve this goal. Each 116 morning, the app issues a set of 5 suggestions. The app then monitors Jane's activities 117 throughout the day and uses that information to choose 5 suggestions for the following day. 118 119 Formally, we will refer to each set of five activity suggestions as an intervention option or

120 *action*. This intervention option or action is the particular choice of the five suggestions. On the

121 morning of day t, the app suggests to Jane the action A_t , where $A_t = [S_{t1}, S_{t2}, S_{t3}, \dots, S_{t10}]^T$ is a

122 10×1 vector of binary variables. S_{ti} has a value of 1 if the *i*-th suggestion from Table 1 is

123 shown to Jane on day t, and 0 otherwise. Thus A_t will have 5 entries equal to 1 and 5 entries

124 equal to 0. Further, let Y_t denote the number of active minutes for Jane on day t, which might be

125 called the *proximal outcome* or *reward* of action A_t .

126

127 Consider the following linear regression model for the mean of the daily active minutes Y_t on 128 day t in terms of the suggestions:

$$E[Y_t|A_t] = \sum_{i=1}^{10} \beta_i S_{ti}$$

$$= \beta^T A_t$$
(1)

129 where the second equality is written more compactly by using vector notation, $\beta =$

130 $[\beta_1, \beta_2, \dots, \beta_{10}]^T$. Here $\beta_1, \beta_2, \beta_3, \dots, \beta_{10}$ respectively represent suggestion 1, 2,3, ..., 10s

131 contribution to Jane's number of active minutes. Therefore, Equation 1 has the following simple

132 interpretation: Y_t , the number of daily active minutes, is the sum of the effects of the 5 activity

133 suggestions provided on day t (i.e., suggestions for which $S_{ti} = 1$).

134

Formally, our goal is to discover the best action $A_t = a^*$ that is, the set of 5 suggestions that

136 makes Jane most active (that results in the highest mean daily active minutes). We can formally

137 write this goal as: given β , determine the action a^* for which

$$\boldsymbol{\beta}^T \boldsymbol{a}^* \ge \boldsymbol{\beta}^T \boldsymbol{a} \tag{2}$$

138 where *a* is a combination of 5 suggestions from Table 1. β is, however, unknown. We can 139 estimate Jane's a^* by running experiments in the following way: at the start of a day *t*, the app 140 selects action A_t (in other words, it delivers to Jane a combination of 5 suggestions from Table 141 1). The tracker then counts the number of minutes Jane is active on the day (note that this 142 number is the proximal outcome Y_t). If the 5 suggestions are useful, then Jane will be more 143 active that day and Y_t will be high compared to other days with a different set of 5 suggestions. Now, the question is: how to select the 5 suggestions each day? One simple approach is to select 144 145 5 suggestions out of 10 with equal probability. But such a uniform selection strategy will select 146 more useful and less useful suggestions equally. A more sophisticated approach is to use the 147 information already available from the past experiments to select future suggestions that will 148 both yield additional information about a^* and give as few less useful suggestions as possible. 149 Note that here we face the same exploit-explore tradeoff faced by the classic bandit setting's 150 gambler - i.e., how to balance exploiting suggestions that seemed useful in the past with 151 exploring less frequently issued suggestions.

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153 An effective approach to delivering less useful suggestions as little as possible is "optimism in 154 the face of uncertainty" epitomized by the Upper Confidence Bound (UCB) technique [7,8]. 155 Bandit algorithms based on the UCB have been well studied and possess guarantees of 156 minimizing the number of less useful suggestions. The key intuition behind the UCB idea is the 157 following: First, for each choice of action a_t , a confidence interval is constructed for the linear combination $\beta^T a_t$. Recall this linear combination represents $E[Y_t | A_t = a_t]$, the expected 158 159 proximal outcome after receiving action, a_t . Then the UCB bandit algorithm selects the action with the highest upper confidence limit. Note that the upper confidence limit for $\beta^T a_t$ can be 160 high for either of two reasons: (1) either $\beta^T a_t$ is large and thus a_t is a good action to make Jane 161 162 active, or (2) the confidence interval is very wide with a high upper limit, indicating that there is much uncertainty about the value of $\beta^T a_t$. Using the upper confidence limit represents UCB's 163 164 optimism; UCB is optimistic that actions with high upper confidence limits will be the best 165 actions, even though a larger upper confidence limit can mean more uncertainty. However, if an

action with high upper confidence is indeed not the optimal action, then selecting the action will
reduce the uncertainty about the effect of this action. This will help UCB realize that the action
is indeed not useful.

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How does UCB choose an action using the upper confidence interval? By following these two steps. The first step involves using Equation 1 to estimate β assuming homogeneous error variance. We might use ridge regression to estimate β because ridge regression regularizes to avoid overfitting, especially when Jane has just begun to use the app and we have less data [8,9]. In this case the estimator of β , denoted by $\hat{\beta}_t$, after t days of using the bandit algorithm is:

$$\widehat{\boldsymbol{\beta}_t} = \widehat{\boldsymbol{\Sigma}}_t^{-1} \left(\sum_{u=1}^t A_u \boldsymbol{Y}_u \right)$$
(3)

where $\hat{\Sigma}_t^{-1} = \sum_{u=1}^t (A_u A_u^T) + I_{10}$ and I_{10} is an 10 × 10 identity matrix. Equation 3 is the standard 175 solution for ridge regression. The second step is to construct an upper confidence limit for $\beta^T a$ 176 for each possible action a; the upper confidence limit on day t for action a is given by $\hat{\beta}_t^T a +$ 177 $\alpha \sqrt{a^T \hat{\Sigma}_t^{-1} a}$, where α is an appropriate critical value. Note, since we assumed homogeneous error 178 variance, $\hat{\Sigma}_t^{-1}$ is proportional to the covariance for $\hat{\beta}_t$, and $a^T \hat{\Sigma}_t^{-1} a$ is the covariance of $\beta^T a$. 179 Thus, $\sqrt{a^T \hat{\Sigma}_t^{-1} a}$ represents standard deviation of $\beta^T a$ and the upper confidence limit of $\beta^T a$ has 180 an interpretable form, which is simply the current estimate, $\hat{\beta}_t^T a$, plus its standard deviation 181 multiplied up to a constant factor α . Then, to choose the UCB action for day t + 1, we calculate 182 183 the a_{t+1} for which

$$\widehat{\beta}_t^T a_{t+1} + \alpha \sqrt{a_{t+1}^T \widehat{\Sigma}_t^{-1} a_{t+1}} \geq \widehat{\beta}_t^T a + \alpha \sqrt{a^T \widehat{\Sigma}_t^{-1} a}$$
(4)

for all actions *a*. i.e., a_{t+1} is selected to maximize the upper confidence limit on the mean of *Y*_{t+1}. This approach possesses strong guarantees to minimize the number of less useful suggestions [8,17].

188

189 Here we summarize how the UCB bandit algorithm works on Jane's smartphone. First there is an 190 "exploration phase" to allow the UCB algorithm to form preliminary estimates of β . This phase 191 lasts for a number of days, say t_0 days, during which each morning the UCB bandit algorithm 192 randomly selects an action, that is, uniformly selects five activity suggestions from the 10, and 193 delivers these suggestions to Jane in the application. Then at the end of day t_0 , the UCB bandit uses an incremental calculation to form $\hat{\beta}_{t_0}$ and $\hat{\Sigma}_{t_0}$ based on the selected action, Jane's activity 194 minutes, Y_{t_0} , for that day and the prior day's $\hat{\beta}_{t_0-1}$ and $\hat{\Sigma}_{t_0-1}$. Next the UCB algorithm 195 calculates the upper confidence limit for each action and selects the action a_{t_0+1} with the highest 196 197 upper confidence limit. On the next morning, Jane is provided the five suggestions as specified by a_{t_0+1} . The UCB algorithm repeats the process by estimating new $\hat{\beta}_{t_0+1}$ $\hat{\Sigma}_{t_0+1}$ and an updated 198 199 set of 5 suggestions are chosen for the next day and so on.

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201 **3.1.1 A simulation example**

In this section, we use a simulated example to demonstrate how a UCB bandit algorithm can personalize suggestions for Jane. We assume the following simple model of how Jane responds to the suggestions: When Jane sees a suggestion, she follows it with probability p or does not follow it with probability 1 - p. If Jane follows the suggestion, she spends D minutes following

206 it on a particular day. We assume D is random and normally distributed, because Jane may not 207 spend the same amount of time each time she follows the same suggestion. In Table 2, we 208 created an artificial example scenario with p and D values for different suggestions. The D209 values are written as mean \pm standard deviation. We also show the expected number of activity 210 minutes that Jane spends following a suggestion when she sees it. This expected number is $p \times E[D] + (1-p) \times 0 = pE[D]$. These expected minutes are also β values in equation 1. Note 211 212 that β values are unknown in real world setting. We use known β values in a simulated example 213 to show how the UCB algorithm finds the suggestions with higher β values.

Suggestions	р	Duration, <i>D</i> (in minutes)	Expected duration <i>pE</i> [<i>D</i>] (in minutes)
1. Walk 30 minutes	1	15 <u>+</u> 4	15.0
2. Add intervals: walk 5 minutes, walk very fast 5 minutes, repeat 3 times	$\frac{1}{90}$	21 ± 5	0.4
3. Take the stairs instead of the elevator whenever possible	$\frac{5}{7}$	7.5 ± 2	5.2
4. Go with a friend or your dog for a walk	$\frac{6}{7}$	22 ± 10	18.9
5. Swim a lap, rest for 1 minute, repeat 10 times	0	_	_
6.Attend a fitness class at your gym	$\frac{1}{14}$	31 ± 5	2.2
7. Try some of the strength training and bodyweight exercises illustrated by the fitness app on your phone	0	_	_

8. Yoga	$\frac{4}{7}$	18 <u>+</u> 3	10.3
9. Park at the far end of the parking lot to walk further	$\frac{4}{7}$	11 ± 2	6.3
10. Do yardwork for at least 10 minutes	$\frac{3}{14}$	24 <u>+</u> 5	5.1

Table 2: A simulated scenario for Jane where *p* represents the probability of following a suggestion when Jane sees it, and if the suggestion is followed, "Duration" represents the number of daily minutes spent following the suggestion. Finally, *p* and "Duration" are used to compute the expected value pE[D], which also represents β values for the suggestion.

219

220 With the above setup, we run the simulation in two stages. In the first stage, suggestions are 221 included with equal probability in the five suggestions on each of the first fourteen days. This 222 initial "exploration phase" helps to form an initial estimate of β . In the second stage, we run the UCB bandit algorithm: on each day, we compute $\hat{\beta}_t$, according to equation 3, and choose an 223 224 action using Equation 4. We run these simulation for 56 days, or 8 weeks. We run 200 instances 225 of the simulation to account for randomness in the problem. One source of this randomness 226 comes from the exploration phase, where the app generates non-identical sequences of random 227 suggestions based on when Jane starts using the app. We deal with this randomness by resetting 228 the randomization seed after each simulation run. Another source of randomness comes from the 229 within-person variability of how Jane responds to the suggestions. We create a second stream of 230 random numbers to simulate how Jane responds to the suggestions. The seed of this second 231 stream remains unchanged after each simulation run; we do not reset this seed because, doing so 232 will add the randomness of resetting the seeds to the within-person variability.

234	Table 3 shows the results, where we report the mean of the β estimates. At the top, we list the
235	actual β values. We then list in each row how many times a suggestion is issued by UCB over a
236	two week period. We use boldface for the top five suggestions (1 st , 3 rd , 4 th , 8 th , 9 th in Table 1).
237	The simulation shows that after the two-week exploration phase, UCB chooses the top
238	(boldfaced) suggestions more times than the less useful ones. Since a suggestion can be picked
239	only once a day, the top suggestions 1, 2, and 8 from Table 3 are picked nearly every day after
240	the exploration phase (11-14 days between week 3-4, 5-6, and 7-8). However, suggestions 3, 9,
241	and 10 all have similar β values. As a result, UCB is often uncertain among them and chooses
242	the 10th suggestion sometimes wrongly, since it is not in the top five suggestions.

243

Suggestions	1	2	3	4	5	6	7	8	9	10
β	15.0	0.4	5.2	18.9	0.0	2.2	0.0	10.3	6.3	5.1
\widehat{N} (week 1-2)	7.1	7.2	7.0	7.0	6.8	6.9	6.9	6.8	7.1	7.1
\widehat{N} (week 3-4)	12.4	3.9	6.3	13.4	2.8	4.5	2.5	9.6	7.8	6.5
\widehat{N} (week 5-6)	12.8	3.5	6.3	13.7	2.6	4.3	1.7	10.1	8.1	6.7
\widehat{N} (week 7-8)	13.1	3.4	6.4	13.8	2.4	4.3	1.6	10.1	7.8	6.8

Table 3: Number of times suggestions are picked by the app within each of the two-week 244

intervals. \hat{N} denotes the number of days the app selects a suggestion in the time frame mentioned 245 246 within parenthesis. Note, the number of times a suggestion can be selected during a two-week period is at most 14 (i.e., $\hat{N} \leq 14$). 247

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3.2. Optimizing interventions for different contexts

252 In the earlier section, we discussed an example of personalizing suggestions with the UCB 253 algorithm. Our goal was to demonstrate the inner workings of a bandit algorithm in a simple 254 setting. Here we discuss extending the prior example to a more realistic setting where we tailor 255 suggestion based on users' context. Indeed, context can determine whether, and the degree to 256 which, certain suggestions are actionable. For example, Jane may only be able to act on the 257 vardwork suggestion on the weekend, or she may appreciate and act on the reminder to take her 258 dog for a walk when the weather is good. By adapting suggestions to different contexts, we hope 259 to enhance her activity level. Fortunately, we can contextualize suggestions by re-purposing the 260 bandit technique described already. We briefly describe one way to do so below.

- 261
- 262

	Context
1	Bad weather, weekend
2	Bad weather, weekday
3	Good weather, weekend
4	Good weather, weekday

263

Table 4: Different types of contexts

264

For clarity, we will first consider a very simple context involving only the weather and day of the week. For these two contexts, there are two states (i) weekend or weekday, (ii) good or bad weather, where we consider the whole day as bad weather if only part is. Thus, each day belongs to one of four different context combinations (see Table 4). Note this simple characterization of 269 only 4 contexts is to convey the idea of contextualization rather than actually to realistically270 handle a large number of contexts.

271

272 For these four context combinations, the task of contextualizing suggestions boils down to 273 optimizing the suggestions for each of the four. An intuitive approach is to use 4 different bandit 274 algorithms, one for each context combination. Depending on the context on day t, the 275 corresponding bandit would be activated for optimizing suggestions for that context. Recall that 276 an action is a set of five activity suggestions from the 10 in Table 1. Each of the four different 277 bandit algorithms uses a model such as Equation 1 but with different β s due to the different 278 contexts. We represent this difference by sub-scripting β as β_k for the *k*-th (k = 1,2,3,4) context. 279 So, the goal is to learn the optimal action a_k^* that maximizes the average number of minutes active for Jane in context k. That is, for k = 1,2,3,4 the goal is to learn the action a_k^* which 280 281 satisfies

282

$$\beta_k^T a_k^* \ge \beta_k^T a_k$$

Again, one UCB bandit algorithm can be run per context to learn the optimal five suggestions forthat context.

285

Note that using a separate bandit algorithm for each context is not a feasible approach in a realworld setting; there are too many possible contexts. It would take the bandit algorithm many days to obtain good estimates of the β_k parameters. However, we can use a few tricks to handle large number of contexts. First, we may know a priori that some suggestions are equally actionable across different contexts and some suggestions are not at all actionable in certain contexts. If the suggestions are equally actionable across contexts, we can use the same

292	β_k parameter values for these contexts. And if a suggestion is not actionable in a given context
293	we can set its parameter in β_k to zero. Second, we can pool information across people. For
294	example, some suggestions, such as yardwork, are more actionable on weekends for most
295	people. Thus, we don't need to find β_k for each user individually. Pooling information, however,
296	requires a Bayesian approach where for a new user, initially β_k is pooled from prior users and
297	once some data from the user is available, β_k is then adapted to make more user-specific
298	changes. Bayesian approaches to bandit algorithms are beyond the scope of this chapter; but the
299	techniques are along the same lines as UCB [10].

300

301 4. A real-world example

302 Earlier, we gave two simple examples of how the UCB bandit algorithm can personalize and 303 contextualize mobile health interventions. Real-world examples, however, are more complicated, 304 with many potential suggestions and many contexts. Below we discuss an mHealth app called 305 MyBehavior that has been deployed multiple times in real world studies [11,12]. MyBehavior 306 utilizes phone sensor data to design unique suggestions for an individual and subsequently uses a 307 bandit algorithm to find the activity suggestions that maximize chances of daily calorie burns. 308 Like the example in Section 3, MyBehavior issues the suggestions once each morning. The 309 number of suggestions, however, is higher than in Table 1 because the suggestions in 310 MyBehavior closely match an individual's routine behaviors, and routine behaviors are dynamic. 311 In the following, we briefly discuss how MyBehavior uses the bandit algorithm. More 312 information on this can be found in [13]. 313

4.1 MyBehavior: Optimizing individualized suggestions to promote more physical activity

The following discussion of MyBehavior first covers how unique suggestions are created for each individual. We then briefly discuss how a bandit algorithm is used to find optimal activity suggestions that have the highest chance of maximizing an individual's daily calorie burn.

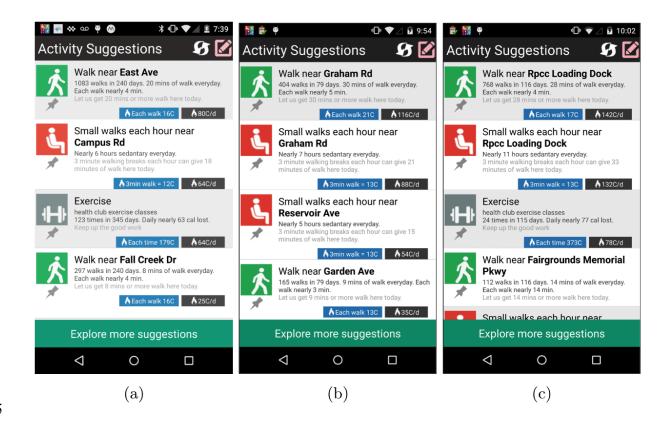
319

320 The MyBehavior app tracks an individual's physical activity and location every minute. The 321 detected physical activities include walking, running, driving, and being stationary. The app then 322 analyzes the location-tagged activity data to find patterns that are representative of the user's 323 behaviors. Figure 1 shows several examples of behaviors found by MyBehavior. Figure 1a and 324 Figure 1b respectively contain places where a user stayed stationary and a location where the 325 user frequently walked. Figure 1c shows similar walking behaviors from another user. 326 MyBehavior uses these behavioral patterns to generate suggestions that are unique to each 327 individual. For example, one intervention may suggest an activity goal at specific locations that 328 the user regularly goes to. Such tailoring makes feedback more compelling, since a user's 329 familiarity with the location enhances adherence [1].



Figure 1: Visualization of a user's movements over a week (a) Heatmap showing the locations
where the user is stationary everyday (b) Location traces of frequent walks for the user (c)
Location traces of frequent walks for another user

335 Specifically, MyBehavior creates three kinds of uniquely individualized suggestions: (i) for 336 stationary behaviors, MyBehavior pinpoints the locations where the user tends to be stationary 337 and suggests taking small walking breaks every hour in these locations. (ii) for walking 338 behaviors, MyBehavior locates the different places the user usually walks and suggests 339 continuing to walk in those locations (iii) for other behaviors, e.g., participation in yoga class or 340 gym exercises, MyBehavior simply reminds the user to keep up the good work. Figure 2 shows 341 several screen shots of the MyBehavior app, where Figures 2a-c are suggestions for three 342 separate users. Since MyBehavior suggestions are tailored to the user, the first suggestion at the top of each screen shot is to walk, but the locations are different. Also, the first and third users 343 344 receive a gym weight training exercise suggestion that the second user does not.



345

346

Figure 2: MyBehavior app screenshots for three different users¹

347

348 Now, how does MyBehavior decide which suggestions to give? MyBehavior uses a bandit 349 algorithm like that in Section 3's first example, where suggestions are issued once a day. But 350 MyBehavior can offer many more suggestions than Table 1 contains, depending on the variety of 351 locations in which a user might be sedentary or active, etc. Fortunately, the bandit algorithm can 352 still efficiently adapt to these high numbers of tailored suggestions. Rabbi et al [13] details how 353 this optimization works, but the key intuitions are the following: (i) Most human behaviors are 354 highly repetitive and routine and occur in the same locations. Routine behaviors and locations 355 will be detected early and thus included soon in the individual's list of suggestions. (ii) The 356 suggestions relating to routine behaviors and locations are more likely to be followed than

¹ Figure 1 and 2 have been reproduced from Rabbi et al. [12] with appropriate permission from the authors.

357 suggestions of non-routine behaviors in non-routine locations. Thus, the bandit will learn about 358 the effects of these suggestions more quickly and these suggestions will likely remain effective if 359 the user's routine does not change.

360

361

362 **5. Discussion**

363 In the last two sections, we discussed several examples of how bandit algorithms can optimize 364 mobile health interventions. The bandit algorithm balances experimenting with different activity 365 suggestions and selecting activity suggestions that currently appear most useful. This balancing 366 act ensures that the algorithm acquires necessary information while maintaining an engaging user 367 experience by providing as few less-useful suggestions as possible. While we showed that bandit algorithms can be useful to personalize and contextualize suggestions, there are additional 368 369 complexities in real-world mHeath intervention settings that generate new challenges for bandit 370 algorithms to address:

371

372 **Ignoring delayed effects**: In bandit algorithms, the optimal action is the action that maximizes 373 the immediate reward (proximal outcome). In other words, bandit algorithms ignore the potential 374 impact of the action on future context and future proximal outcomes. Some actions, however, 375 can have long-term negative effects even if the short-term effect is positive. e.g., delivering an 376 office walking suggestion may increase a user's current activity level, but the user might become 377 bored after repeating the office walk several days, thus future suggestions may be less effective. 378 In these cases, other algorithms that explicitly allow past actions to impact future outcomes [14] might be used. Precisely, the outcome of these algorithms are $Y_t + V(X_{t+1})$, where $V(X_{t+1})$ is 379

the prediction of the impact of the actions on future proximal outcomes given the context X_{t+1} at the time t + 1 (a bandit algorithm acts as if $V(X_{t+1})=0$). These algorithms tend to learn more slowly than bandit algorithms, since we need additional data to form the prediction $V(X_{t+1})$. We conjecture that the noisier the data is, the harder it will be to form high quality predictions of $V(X_{t+1})$ and thus as a result, bandit algorithms may still be preferable.

385

386 Non-stationarity: Most bandit algorithms assume "stationary" settings; i.e., the responsivity of a 387 user in a given context to an action does not change with time. This assumption can be violated 388 in real-word settings; in MyBehavior, for example, we observed that many suggestions become 389 ineffective when people switched job and moved from one location to another. Such changes 390 over time are often referred to as "non-stationarity." Other types of non-stationarity can be 391 caused by life events such as a significant other's illness or aging. Bandit algorithms are typically 392 slow to adapt to non-stationarity. Speeding up this process is a critical direction for future bandit 393 research.

394

Dealing with less data: In real world applications, where the number of contexts and actions are many, bandit algorithms will need a lot of burdensome experimentation to find the optimal action for a given context. One way around this is to use a "warm start." A warm start set of decision rules that link the context to the action can be constructed using data from microrandomized trials [15] involving similar individuals. Recently Lei et al. [16] developed a bandit algorithm that can employ a warm start. However, we still need to test whether, and in which settings, warm starts will sufficiently speed up learning.

403	Adverse effects: Since mHealth interventions are generally behavioral, the risk of personal harm					
404	is often minimal. Nonetheless, there could be potential iatrogenic effect because phones cannot					
405	capture every piece of contextual information and bandit algorithms ignore the long-term effects					
406	of interventions. Since bandit algorithms don't take interventions' long-term effects into account,					
407	the algorithm may notify or otherwise deliver interventions too much and thus cause annoyance					
408	and reduce app engagement. Future work needs to investigate how to account for such long-term					
409	adverse effects. Furthermore, current phone sensors cannot automatically capture critical					
410	contextual information such as a user's health risks, preferences, barriers, emotional states, etc.					
411	Incomplete information may cause the algorithm to provide less appealing (e.g., not suggesting					
412	an activity that a user likes but didn't do often in the past) and inappropriate suggestions (e.g.,					
413	asking someone who is injured to walk). Providing human control over the suggestion					
414	generation process can mitigate these problems; e.g., a user can delete inappropriate suggestions					
415	and prioritize the suggestions that are more appealing [12].					
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